Did the MPs' voting pattern in the indicative votes on Brexit have any structure? Christian List and Kai Spiekermann

Draft of 31 March 2019

On 27 March 2019, Parliament held indicative votes on eight different Brexit options:

- Baron: No Deal
- Fysh: Managed No Deal
- Eustice: Efta and EEA
- Boles: Common Market 2.0
- Clarke: Customs union
- Corbyn: Labour's plan
- Beckett: Confirmatory public vote
- Cherry: Revoke to avoid No Deal

MPs were able to cast votes on all of these options. Rather than ranking the options in an order of preference, MPs were asked to vote for as many or as few options as they liked. For each option, they could indicate their approval or disapproval (with abstention allowed). Thus, they were asked to cast what social choice theorists call "approval ballots". In this context, a vote for any given option is best interpreted as expressing an opinion to the effect that this option is in principle acceptable (even if it may not be the relevant MP's most preferred option).

From a political-science perspective, whenever some individuals vote on several options, it is interesting to ask whether there is any systematic structure in their pattern of votes. For example, we may ask whether those votes can be explained in terms of disagreements about the ideal position on some underlying political dimension (the simplest example of such a dimension being the conventional socio-economic left-right dimension).

If MPs had ranked the options in a complete order of preference (indicating their most preferred option, their second most preferred option, their third most preferred option, and so on), we would have been able to analyse whether their preferences were "single-peaked". That is to say, we would have been able to ask whether the options can be arranged on a single left-right axis such that each MP has a most preferred position somewhere on that axis with decreasing preference for options as they get more distant in either direction from his or her most preferred position.¹ (Of course, the left-right axis here need not necessarily coincide with the conventional socio-economic left-right dimension.) More generally, we might have been able to look for single-peakedness within some multi-dimensional political space. Given the kinds of votes that were cast, however, this analysis is not possible (and certainly not without some further *ad hoc*

¹ For an example of this kind of analysis, see List, Luskin, Fishkin, and McLean, "Deliberation, Single-Peakedness, and the Possibility of Meaningful Democracy: Evidence from Deliberative Polls", *Journal of Politics*, 2013.

assumptions). The notion of single-peakedness is not applicable in the case of approval ballots of the present kind.

But there is another structural condition that is applicable in the present context, and that is the notion of "unidimensional ordering". A combination of approval ballots on some options across a set of voters is called "unidimensionally ordered" if and only if the following pattern holds:

The voters (not the options) can be aligned from left to right on a single axis such that, for each option under consideration, the voters approving that option form an adjacent block on that axis. (Adjacency of the voters approving an option simply means that whenever voters *i* and *j* approve a particular option, then all voters who lie in between *i* and *j* on the given axis also approve that option.)

As in the case of single-peakedness, the notions "left" and "right" are used in a purely geometrical sense here: "left" and "right" can in principle have many different interpretations. In the case of Brexit, the alignment of voters could be from most pro-Brexit to most pro-Remain, for example.

The following simple example with nine voters and five options illustrates what a profile of unidimensionally ordered approval ballots might look like.

	Voter 1	Voter 2	Voter 3	Voter 4	Voter 5	Voter 6	Voter 7	Voter 8	Voter 9
Option 1			Approve	Approve	Approve				
Option 2	Approve	Approve	Approve						
Option 3							Approve	Approve	Approve
Option 4			Approve	Approve	Approve	Approve	Approve		

Table 1: An Example of Unidimensional Ordering

We can think of "unidimensional ordering" as corresponding to a certain kind of "metaconsensus": a consensus, not on which option to approve, but rather on an underlying normative or cognitive dimension that structures the disagreement between the voters.

When a combination of approval ballots is "unidimensionally ordered", this has two significant implications from a social-choice-theoretic perspective:²

(1) The set of majority-approved options is always a subset of the set of options approved by the median voter with respect to the given left-right alignment. In the example of Table

² See Dietrich and List, "Majority Voting on Restricted Domains", *Journal of Economic Theory*, 2010, where the notion of "unidimensional ordering" was first defined, extending the definition of "unidimensional alignment" in List, "A Possibility Theorem on Aggregation over Multiple Interconnected Propositions", *Mathematical Social Sciences*, 2003.

1, the median voter is voter 5, and indeed there are two majority-approved options here, namely options 4 and 5. Both are approved by the median voter.³

(2) If there are any logical relationships between the options (so that some combinations of options are mutually inconsistent in the sense that it would be irrational to approve them simultaneously as being acceptable), the set of majority-approved options is consistent, as long as the median voter is consistent in his/her set of individual votes across the options. (This is particularly relevant when collective decisions are made on multiple related proposals and we are looking for an overall consistent package of decisions.)

Implication (1) means that, given unidimensional ordering, only those options that are interpretable as a centrist compromise (by being approved by the median voter on the relevant left-right axis) have a chance of being majority-approved. Implication (2) means that unidimensional ordering is sufficient for consistent majority decisions in those cases where there are mutual compatibility constraints between the options. (In general, as is well known, majority voting does not ensure consistent outcomes across multiple options, and so it is significant that unidimensional ordering implies that the majority outcome will be consistent.)

We looked at whether the MPs' indicative votes on 27 March 2019 were unidimensionally ordered. Specifically, we focused on all those MPs who did not universally abstain (i.e., those who voted either "yes" or "no" on at least one of the eight options). The total number of MPs considered on the basis of this criterion was 602.

What were our results?

First of all, we were not able to arrange *all* of the 602 MPs on a single left-right axis such that the pattern of unidimensional ordering was satisfied. In that sense, Parliament as a whole lacks a meta-consensus. There is not only no agreement on which options to approve (i.e., no

³ Note that when a given combination of approval ballots is unidimensionally ordered, the left-right axis with respect to which the relevant pattern holds may not be unique. Therefore, the median voter may not be unique either. Crucially, however, the claim that the set of majority-approved options is a subset of the set of options approved by the median voter is true *for any left-right axis with respect to which the relevant pattern holds*. Furthermore, there is an important special case of unidimensional ordering, called "unidimensional alignment", in which some of the present claims can be strengthened. (See the previous footnote for references.) A combination of approval ballots is called "unidimensionally aligned" if and only if the following pattern holds: the voters can be aligned from left to right on a single axis such that, for each option under consideration, the voters approving that option lie on the opposite side of those not approving it. Note that unidimensional alignment implies unidimensional alignment), but the converse does not hold (insofar as the set of voters approving a given option may form an adjacent block, but this block may be surrounded on both sides by voters not approving the option). When a combination of votes is unidimensionally aligned, the set of majority-approved options is not merely a *subset* of the set of options approved by the median voter, but it *coincides* with the set of options approved by the median voter.

"substantive consensus"), but also no agreement on a single shared dimension structuring the MPs' disagreement in a unidimensionally ordered form (i.e., "no meta-consensus").⁴

Secondly, however, there was a significant "proximity to unidimensional ordering", meaning that we were able to arrange a significant number of the MPs (namely, 511 of them) on a single left-right axis such that their voting pattern was unidimensionally ordered.

The table on the following page (Table 2) describes the way in which 511 MPs can be arranged from left to right so as to subsume their votes under the pattern of unidimensional ordering. As in Table 1, rows represent options, and columns represent voters, here: groups of MPs. Each column lists a group of MPs who approved the same set of options. For each option, the highlighted region in green corresponds to the group(s) of MPs who voted in support of that option. Subsequently, for completeness, we also include a list of all MPs whose votes did not fit into this pattern, namely 91 out of 602 (Table 3).

Although one must be cautious not to over-interpret the present results, there are some potentially useful lessons to be learnt here.

First of all, the MPs' voting pattern is closer to a unidimensional structure than one might have expected. As many commentators have noted, Parliament is extremely fragmented. Yet, approximately 85% of the non-abstaining MPs (namely, 511 out of 602) can be systematically aligned on a single axis such that their voting pattern across all eight options comes out as "unidimensionally ordered".

Secondly, the identified alignment of MPs allows us to visualize in simple terms which MPs have relatively similar positions across the eight options (insofar as they are close to one another on the relevant axis), and which MPs have relatively distant positions. Presumably, MPs with relatively similar positions will more easily be able to find some common ground and agree on certain compromise positions. Our table further suggests that, at least as far as the voting pattern is concerned, it may be possible to achieve a majority on some compromise options by combining adjacent voting blocks.

Finally, the options approved by the median voter on the given alignment have the greatest chance of achieving majority support, after further deliberation and negotiation. (Of course, right now, no option commands a majority.)

It will be interesting to discuss whether any additional lessons can be learnt from the analysis.

⁴ On the distinction between substantive and meta-agreement, see List, "Two Concepts of Agreement", *The Good Society*, 2002.

								4	Alan Duncan, Mike Freer, Angus Brendan MacNeil, Pete Wishart	
								з 64	Heid Allen, Hannah Bardel, Luciana Berger, Mhairi Black, Ian Black ford, Kisty Blackman, Tom Brake, Deidre Brock, Alan Bown, Vince Cable, Lias Cameron, Alista IC Camrichel, Douglas Chapman, Jannan Denry, Ann Ourd, Ann Coffer, Komic Couns, Angela Cawley, Edward Daver, Martyn Day, Martin Docherny-Hughes, Tim Farron, Marion Felows, Mile: Gapes, Stephen Ceiffins, Parkici Gabon, Parici Cani, Cadi, Peter Grani, Hei Gran, Justite Ceieming, Dominic Grieve, Drew Hendry, Lady Hermon, Wera Hobhoue, Stewart Hoss, Christine Jantike, Minist Jaw, Pillei Le, Ortis Leil, David Linden, Carolle Lucas, Schlahn McConals, Stewart Malcolm McConald, Staur CL, McConald, Carol Mongahan, Layla Moran, Gavin Revelands, Bendan Dikar ¹ , Jano Ryan, Tommy Steppang, Gavin Shackar, Angela Shah, Noem Shith, Anna Souby, Chris Stephens, Janies Stone, Ja Switson, Alison Thewliss, Chulia Limunana, Pillipas Mindrod, San J Wordson, Jan Woodcock, Daviel Zeichner David Lammy, Anna McMornin, Paul Williams	
								50	Rosena Allin-Khan, Tonia Antoniazi, Ben Bradshaw, Lyn Brown, Karen Buck, Ruth Cadbury, Neil Coyle, Mary Creagh, Stella Creasy, Janet Daby, Genant Davies, Mansha De Cordova, Emma Dent Coad, Stephen Doughty, Rose Duffield, Maria Eagle, Angele Eagle, Loaise Elman, Chris Einnon, Ruth Goroge, Prevert Kar util, Nate Green, Lillan Generwood, Fahan Insmithon, Helen Haves, Mag Hiller, Margaret Hodge, Rupa Huo, Darren Iones, Suta Faha Insmithon, Nelen Haves, Kothe Lewis, Rachela Maskell, Christian Matthews, Kerry M Cathry, Charlene M Kofmich, Madelene Moon, Stephen Morgan, Nate Otamor, Ellie Reeves, Lioyd Ruszek-Moyle, Banry Sheeman, Tulp Siddig, Andy Slaughter, Wes Streeting, Anna Turley, Thelma Waker, Catherine West, Martin Whitfield	
								50	Rushanara Ali, Cive Betts, Roberta Blackman-Woods, Paul Biomfeld, Kevin Biennan, Bambos Charalmboso, David Casuby, Alex Canningham, Thangam Debbonaile, Anneliese Dodds, David Drev, Oter Efford, all Estsonso, Paul Fanely, Vely Concolt, James Frith, Nath Gaffey, Roger Godsff, John Grogan, Louize Hagh, Jiarriet Human, Geoge Howardt, Sanh Jones, Peter Yey, Leisley Laidt, Shahana Mahmood, Sandy Marin, Chi Orouzni, Aberd Dowe, Matthew Pennycood, Jess Phillips, Like Poland, Faisali Rashid, Steve Beed, Rache Heeves, Matte Rimmer, Matt Rodda, Daniele Rovely, Viende Jasima, Jeff Smith, Kains Nyth, Alex Sole, Paul Sweeney, Gareth Thomas, Stephen Timms, Stephen Tivigg, Keith Vaz, Matt Western, Alan Whitehead, Mohammad Yasin	
								67	Diane Abbott, Mike Amesbury, Jonathan Ashworth, Adfain Balley, Hilary Benn, Nicholas Brown, Chris Bryant, Richard Burden, Richard Burgon, Liam Byrne, Dan Carden, Jenny Chapman, Vernon Cakler, Yvette Cooper, Jerster (cohry, John Cyrer, Wayne David, Taramapier Singh Dhesi, Peter Dowd, Jack Dromey, Colleen Fletcher, Gill Funiss, Helen Goodman, Nia Griffith, David Harson, Emma Hardy, Suce Hayman, Shanon Hodgison, Rate Hollern, Imran Hussain, Dama Johnoo, Gerald Jones, Afail Johan, Tony Liyd, Rehecca Long Bailey, Jan C. Lucas, Holy Lynch, Naidi Mahimood, Sama Mahora, Goodm Marden, Steve Hoc Kobe, Andy McChaola, John McDornell, Coror McGine, Edward Milland, Alex Hons, Toby Perkins, Luan Piccock, Stephen Dundu, Luip Power, Jasmi Careth, Jange Bayner, Christian Res, Emma Brynolds, Jonthan Reynolds, Geoffrey Robinson, Chris Raame, Naz Shah, Cat Smith, Eleano's Smith, Kei Starmer, Fmihy Thomberny, Kai Tumer, Li Twaki Vainéri Naz, Ton Wanon, Pill Wilson, Pill Wilson	
								22	Ian Austin, Tracy Brabin, Julie Cooper, Jon Cruddas, Gloria De Piero, Chris Evans, Mary Glindon, Andrew Gwynen, Carolyn Harris, Dan Janvis, Helen Jones, Mille Kane, Ivan Lewis, Justin Maddes, J.E. McInnes, Jim McMahon, Jan Mearns, Melanie Onn, Stephanie Peacock, Jo Platt, Paula Sherrif, Jon Trakett	Median
								16 4	Richard Benyon, Vicky Ford, Margot James, Nicholas Soames Nick Boles, Steve Brine, Alstair Burt, Stephen Crabb, Jonathan Djanogly, George Freeman, Nick Herbert, Simon Hoare, Jeremy Lefroy, Oliver Letwin, Paul Masterton, Nicky Morgan, Robert Neill,	
								10	Mark Pawsey, Caroline Spelman, Edward Vaizey Bim Afolami, James Cartlidge, Damian Collins, Alberto Costa, Robert Halfon, Simon Hart, Kevin Hollinrake, Rebecca Pow, John Stevenson, David Tredinnick	
								20 7	Peter Aldous, David Duguid, Luke Graham, Bill Grant, Stephen Kerr, Mark Pisk, Gany Streeter Nigel Adams, Kemi Badenoch, Gregory Campbell, Nigel Dodós, Jeffrey M. Donakison, Michelle Donelan, Philip Dunne, Paul Griuran, George Hollingkery, Alaster Jack, Pauline Latham, Emma Little Pengely, Lanakej, Chris Phili, Guirk Robisson, Jim Shannon, David Simpson, Graham Stringer, Theresa Villers, Sammy Wilson	
								66	Adam Afriyie, David Amess, Stuart Andrew, Richard Bacon, Steve Baker, Henry Bellingham, Crispin Blunt, Peter Bone, Ben Bradley, Suella Braverman, Jack Brenton, Andrew Bridgen, Fona Bruce, Coror Barrs, Willam Casi, Christopher Chope, Simon Clark, Geofffrey Cliffon-Brown, David T. C. Davies, Philip Davies, Caroline Dienagea, Naiden cortes, Steve Dode Africhard Drax, James Dudridge, Jain Durans Tmith, Charlie Elphikee, Ngel Evans, Michael Fabricant, Mak Francos, Manzur Shy, Za Coldomh, Jimas Gray, Chris Greun, Mak Harge, Rebeace Jantes, John Hayes, Rate Hoey, Philip Holdoone, Adam Holloway, Eddle Hughes, Ramil Jaywardena, Bermard Jenkin, Andrea Jenkrys, Bosin, Shonion, Carter Johnson, Oarth Johnson, Carbito Johnson, Carter Johnson, David Jones, Mark Lanaster, Edward Leigh, Andrew Lewer, Jalian Lewis, Jula Lope, Janathan Lodi, Tim Loughton, Cing Machilen, Rachel Macale, Amer Maha, Ana Ma, Kiz Mahabone, Faul Maynard, Stephen McPartand, Esther McVey, Stephen Metcalle, Maria Miler, Ngel Mills, Sheryl Muray, Matthew Offord, Philead Joeen Patercon, Ortsober Princher, Tom PungDore, Will Quince, Dominic Raab, Jacob Rees-Mog, Laurence Robertson, Andrew Rosidell, Lee Rowley, Paul Zulv, Gan Shaga, Chenry Smith, Andrew Stephenson, Bob Steward, Lan Stevard, Gaham Stuard, Rahi Suraok, Deximod Swayne, Ross Thomson, Jactis Drinnison, McHarel Tominson, Amer Marin Tander Vara, Gles Warbaron, Jackis Warter, Jan Stevard, Gaham Stuard, Rahi Suraok, Bernond Swayne, Ross Thomson, Jackis Warter, Westler Unders, Andrew Merker Trevela, Na Janek Vara, Gles Warting, Helen Whately, Heather Wheeler, John Whittingdale, Bil Wiggin, William Wragg	
								40	John Baron, Jake Berny, Rehman Chishti, Tracey Crouch, Mims Davies, David Davis, Jackie Doyle- Price, Michele Ellis, Nuora (Ghani, Robert Goodwill, Andrew Griffiths, Onris Heaton-Harris, Robert Jenrich, Marcus Jones, Daniel Kawarynski, Greg Knight, Kwasi Swatere, Jan Liddel-Granger, Jack Loperst, Markensei, Johnny Mercer, Ananda Miller, Janne Mark Morts, James Morris, Wendy Morton, Andrew Murrison, "Nei Oliteri", Mike Pennile, Mark Pittchard, John Redwood, Bob Sceyl, Mark Speers, Rohert Syms, Magler Huroux, Rei Yafhurat, Craig Tacey, Martin Vickers, Matt Waman, Craig Whittaker, Mike Wood	
								55	Edward Argar, Victoria Atkin, Hurriett Baldwin, Paul Berestford, Peter Rottomiley, Andrew Bowle, Graham Bady, Andere Backland, Alex Banginar, Ja Churchli, Chur, Churc, Burce, Chery, Thir?se Caffer, Oliver Douden, David Sennent, Frank Field, Lury Frazer, Roger Cale, Nick Gab, Chayi Gillan, John Gien, Richard Gasham, Helen Grant, Korstene Hair, Luke Hal, Greg Hands, James Heapper, Piter Hearton-Jones, Stephen Hepdum, John Nowel, Rigel Huddieston, Nick Hurd, Andrew Solves, Gillan Keegan, Seema Kennedy, John Lunont, Patrick McQapilin, Damien Moore, Duvid Monis, Jesen Nama, Keth Simpson, Chris Skifmore, Choles Smith, Mel Stide, Rigo Swint, Form Izgendha, Christ Warker, Robin Walker, Kahim Zahawi	
Baron: No Deal	Fysh: Managed No Deal	Eustice: Efta & EEA	Boles: Common Market 2.0	Clarke: Customs Union	Corbyn: Labour's Plan	Beckett: Confirmatory Public Vote	Cherry: Revoke To Avoid No Deal	Votes in Group		

						•			
Baron	Fysh	Eustice	Boles	Clarke	Corbyn	Beckett	Cherry	Size	MPs
									Debbie Abrahams, Margaret Beckett, Dawn
									Butler, Alan Campbell, Nic Dakin, Julie Elliott,
									Barry Gardiner, Margaret Greenwood, John
									Healey, Graham P Jones, Barbara Keeley,
									Karen Lee, Pat McFadden, Alison McGovern,
									Jessica Morden, Teresa Pearce, Bridget
0	0	0	0	1	1	1	0		Phillipson, Nick Smith, Mark Tami, Nick Thomas-Symonds
0	0	0	0	1	1	1	0		Sarah Champion, Rosie Cooper, Judith
									Cummins, Jim Fitzpatrick, Yvonne Fovargue,
									Mike Hill, Kevan Jones, Emma Lewell-Buck,
									Ruth Smeeth, Laura Smith, Gareth Snell, John
0	0	0	0	1	1	0	0	14	Spellar, Derek Twigg, Chris Williamson
									Bob Blackman, Maria Caulfield, Robert
									Courts, Chris Davies, Glyn Davies, Gordon
									Henderson, Scott Mann, Neil Parish, Derek
1	1	1	0	0	0	0	0	10	Thomas, David Warburton
									Kevin Barron, Alex Chalk, Oliver Heald, Anne
0	0	0	0	1	0	0	0	6	Milton, Victoria Prentis, Rory Stewart
1	0	1	0	0	0	0	0	-	Ronnie Campbell, Kevin Foster, Trudy
1	0	T	0	0	0	0	0	5	Harrison, Dan Poulter, Ben Wallace Michael Fallon, Mark Garnier, Julian Knight,
o	1	1	0	0	0	0	0	4	Julian Sturdy
Ŭ	-	_	Ū	Ŭ	Ŭ	Ū	Ū		Jonathan Edwards, Ben Lake, Liz Saville
0	0	0	1	0	0	1	1		Roberts, Hywel Williams
0	0	0	0	0	1	0	0	3	Caroline Flint, John Mann, Grahame Morris
1	1	1	1	0	0	0	0	3	George Eustice, John Penrose, Andrew Percy
0	0	0	0	0	0	1	0		Sam Gyimah, Joseph Johnson
0	0	1	0	1	0	0	0		Damian Green, Sarah Newton
0	0	0	1	1	1	0	1		Kenneth Clarke, Lisa Nandy
0	1	0	0 0	1	0	0	1		Mark Field
0 0	0	1	1	1	0 0	1	1		Guto Bebb Fiona Onasanya
0	0	0	1	0	1	1	0		Jim Cunningham
0	0	0	1	1	0	1	0		Norman Lamb
0	0	0	1	1	0	0	1		Richard Harrington
0	0	0	1	1	0	1	1		lan Murray
0	1	0	1	1	1	0	0	1	lan Lavery
0	0	1	1	1	0	1	0	1	Antoinette Sandbach
0	0	1	1	1	0	0	1	1	Stephen Hammond
0	0	1	1	1	1	0	0		Stephen Kinnock
0	0	1	1	1	1	0	1		Stephen Lloyd
0	0	1	1	1	1	1	1		Mark Hendrick
1	0	0	0	0	0	1	0		Huw Merriman
1	1 0	0	0	1	0	0 0	0 0		Andrew Mitchell Dennis Skinner
1	U	1	U	U	T	U	U	1	Dennis Skiller

6

Table 3: MPs whose votes do not fit into the unidimensional ordering