

# EC102: Market Institutions and Efficiency

## Double Auction: Experiment

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MT 2017



## A Double Auction Experiment

Next we run a market experiment in which:

- participants are partitioned into buyers and sellers;
- buyers and sellers submit bids and offers in any order.

This market game is known as a **double auction** as players on both sides of the market simultaneously submit price quotes.

### Learning Objectives

Understanding experimental trading data.

Understanding market predictions of classical pricing theories.

Relating trading data to predictions of classical pricing theories.

### Outline for Today

- 1 The Double Auction framework.
- 2 Preparation & Experiment.

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### Key References

The first laboratory experiment of double auctions appears in:

- An Experimental Study of Competitive Market Behavior, Smith (1962), Journal of Political Economy.

Laboratory double auction experiments are surveyed in:

- Experimental Economics, Davis and Holt (1993), Princeton University Press.
- Markets, Games and Strategic Behavior, Holt (2006), Addison-Wesley.

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# The Double Auction

## Our Double Auction Specification

### Rounds

- The experiment consists of **3 trading** periods or rounds.

### Roles

- Please **form teams** of three people around you.
- Each team will either be a buyer or a seller in all rounds.

### Actions

- Buyers submit prices to buy units of a commodity.
- Sellers submit price offers to sell such units.

Refer to:

- buyers' submissions as **bid prices**;
- sellers' offers as **ask prices**.

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## Roles: Sellers

Sellers can to produce **at most 3 units** at given monetary costs

$$c_1 \leq c_2 \leq c_3.$$

On each unit sold, a **seller earns the difference between the selling price and the cost** of that unit:

$$\text{Sell 1: } \pi_1^s = p_1 - c_1;$$

$$\text{Sell 2: } \pi_2^s = p_2 - c_2 + \pi_1^s;$$

$$\text{Sell 3: } \pi_3^s = p_3 - c_3 + \pi_2^s.$$

So, high prices and low costs are good for sellers.

When the market opens:

- Sellers submit ask prices at which they are willing to sell units.
- The **ask price** on a unit must be **no lower than its cost!**

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## Roles: Buyers

Buyers value **at most 3 units** at given monetary costs

$$v_1 \geq v_2 \geq v_3.$$

On each unit bought, a **buyer earns the difference between** the monetary **value and** the buying **price** of that unit:

$$\text{Buy 1: } \pi_1^b = v_1 - p_1;$$

$$\text{Buy 2: } \pi_2^b = v_2 - p_2 + \pi_1^b;$$

$$\text{Buy 3: } \pi_3^b = v_3 - p_3 + \pi_2^b.$$

So, low prices and high values are good for buyers.

When the market opens:

- Buyers submit bid prices at which they are willing to buy units.
- The **bid price** on a unit must be **no higher than its value!**

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## Price Revisions & Information

Buyers can revise a bid on any unit at any point ( $\uparrow$  or  $\downarrow$ ).

Sellers can revise an ask on any unit at any point ( $\uparrow$  or  $\downarrow$ ).

The option to revise prices in either direction permits to:

- correct an errors or;
- essentially withdraw a bid ( $\downarrow$ ) or withdraw an ask ( $\uparrow$ ).

The program will display:

- the **highest outstanding bid** to buy;
- the **lowest outstanding offer** to sell.

The lowest ask always exceeds the highest bid.

The difference between the lowest bid and the highest ask is known as to the **bid-ask spread**.

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## Transactions

### Making a Trade: Buyers

A buyer buys a unit by entering a **bid price**  $\geq$  a **seller's ask price**.

If so, the buyer:

- purchases the unit;
- **pays the lowest** outstanding **ask price**.

### Making a Trade: Sellers

A seller sells a unit by entering an **ask price**  $\leq$  a **buyer's bid price**.

If so, the seller:

- sells the unit;
- **is paid the highest** outstanding **bid price**.

### Outstanding Bids and Offers

A transaction cancels all prior bids and offers made on **transacted units**.

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## Examples & Preparation

## Example: First Trade

Consider the following sequence of submissions:

- Buyer  $A$  makes a bid of 1.
- Seller  $A$  makes an offer of 3.
- Buyer  $B$  first bid 1.5 and then raises to 2.
- Seller  $B$  accept by making an offer at 2.

When buyer  $B$  trades with seller  $B$ :

- Both bids of buyer  $B$  would be removed.
- If  $v_1^B = 6$ , then buyer  $B$  would earn 4.
- If  $c_1^B = 1$ , then seller  $B$  would earn 1.
- The highest bid remains buyer  $A$ 's original bid of 1.
- The lowest offer remains seller  $A$ 's original ask of 3.

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## Example: Subsequent Units

Some **participants may** be trying to **trade their first units while others** are trying to **trade their second units**.

For instance, after the first trade:

- Seller  $B$  would attempt to trade the second unit.
- Seller  $A$  would attempt to trade the first unit.
- If  $c_2^B = k$ , seller  $B$ 's next offer would have to be at least  $k$ .
- If  $c_1^A = 1$ , seller  $A$ 's next offer would have to be at least 1.

... and analogously for buyers.

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## Practice Questions

Q1: Suppose that the market period begins with buyer A bidding \$1 for first unit. Which is correct?

- (a) The next submission must be a bid above \$1.
- (b) The next submission may come from any buyer or from any seller, or it may consist of a seller accepting the buyer's bid.

Q2: Let lowest bid be \$7. A seller plans to accept this by entering an ask of \$7. Before entering the ask, however, a second buyer bids \$7.5. The seller, not knowing this, still enters the ask of \$7. The seller would, of course, prefer to sell at the higher bid price. At what will the unit sell for?

- (a) \$7.5
- (b) \$7.0

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## Trading Details: Buyers

Enter your price (dollars and cents) in the bid/ask column.

Bid and ask prices may differ for each unit traded.

**But you must trade your first unit before your second...**

You will see a submit box in the bid/ask column for the following unit only upon trading the previous unit.

	value	bid/ask	price	earnings
unit 1	\$11	\$8.10	\$7.50	\$3.50
unit 2	\$9	<input type="text"/>		\$0.00
unit 3	\$3			\$0.00

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## Trading Details: Sellers

Enter your price (dollars and cents) in the bid/ask column.

Bid and ask prices may differ for each unit traded.

**But you must trade your first unit before your second...**

You will see a submit box in the bid/ask column for the following unit only upon trading the previous unit.

	cost	bid/ask	price	earnings
unit 1	\$3	\$5.10	\$6.50	\$3.50
unit 2	\$3	<input type="text"/>		\$0.00
unit 3	\$9			\$0.00

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## Reminders and Final Details

### Values and Costs

All values have been determined randomly, and may differ across buyers.

All costs have been determined randomly and may differ across sellers.

### Bids and Asks

A bid must be no higher than the buyer's value.

An ask must be no lower than the seller's cost.

### Resubmissions

A trade between a buyer and a seller cancels of all prior bids and asks for that unit, while all the other bids and asks still stand.

### Rounds

Each trading round will last **10 minutes**.

After that, per-round earnings are calculated and a new round begins.

We will keep track of the time and announce remaining time.

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# The Experiment

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## Getting Started

There will be 3 markets:

- Downstairs right – Session Name:
- Downstairs left – Session Name:
- Upstairs – Session Name:

Next please:

- Choose a mobile device of a team member.
- **Turn-off bluetooth and mobile hotspot**, and **close apps**.
- **Connect to** the wifi via **eduroam** (LSE credentials).
- **Go to [veconlab.econ.virginia.edu/login.htm](http://veconlab.econ.virginia.edu/login.htm)**.
- Login with the correct session name and setting a password.
- Quickly run through the instructions.

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# Round 1

Start: **10 Minutes** to Trade

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# Round 1

Middle: **5 Minutes** to Trade

# Round 1

End: **1 Minutes** to Trade

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# Round 1

**Market Closed**

# Round 2

Start: **10 Minutes** to Trade

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# Round 2

Middle: **5 Minutes** to Trade

# Round 2

End: **1 Minutes** to Trade

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# Round 2

**Market Closed**

# Round 3

Start: **10 Minutes** to Trade

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# Round 3

Middle: **5 Minutes** to Trade

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# Round 3

End: **1 Minutes** to Trade

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# Round 3

**Market Closed**

# EC102: Market Institutions and Efficiency

## Double Auction: Results

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MT 2017



## Outline for Today

- Classical Models of Centralized Markets:
  - Competitive Prices;
  - Efficient Trade.
- Classical Models of Decentralized Markets:
  - Local Prices;
  - Price Dispersion;
  - Inefficient Trade.
- Experimental Evidence:
  - Prices and Trade Volume;
  - Convergence to Competitive Equilibrium;
  - Welfare and Comparative Statics;
  - Centralized vs Decentralized Markets.

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- An Experimental Study of Competitive Market Behavior, Smith, Journal of Political Economy 1962.
- Price Dispersion, Hopkins, New Palgrave Dictionary of Economics, 2nd Edition 2008.
- Search and Price Dispersion, Shum, Mimeo 2011  
<http://people.hss.caltech.edu/~mshum/ec105/matt12.pdf>
- Frictional Matching Models, Smith, Annual Reviews 2012.
- The Oxford Handbook of Economics of Network, Organizations and Markets, Part VI 2016.
- The Handbook of Experimental Economics Results, Plott & Smith North Holland 2008.

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## Competitive Markets

## Centralized Markets: Market Clearing & Invisible Hand

In our experimental setting, for any price  $p$ :

- **supply** amounts to **the number of units with cost below  $p$** ;
- **demand** amounts to **the number of units with value above  $p$** .

As we saw in Problem Set 1, this is the case as:

- unit costs are increasing;
- unit values are decreasing.

**Classical Competitive Equilibrium Models** presume that:

- the **market** for all commodities is **centralized**;
- traders maximize payoffs and **take prices as a given**;
- **prices** are determined so to have **demand equal supply**.

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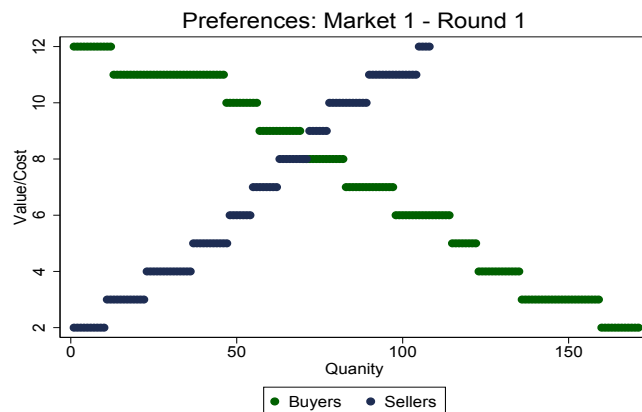
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## Competitive Equilibrium: Market 1 - Round 1

Both values and costs were distributed in  $[2, 12]$ :

- there were approximately 170 units demanded;
- there were approximately 110 units supplied.



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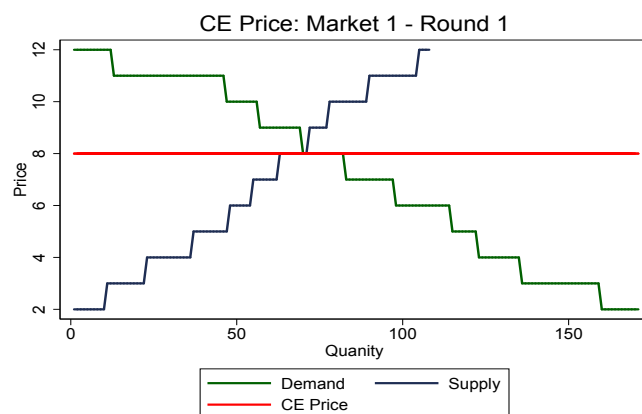
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## Competitive Equilibrium: Market 1 - Round 1

By setting demand equal to supply, we find:

- the competitive equilibrium price  $p^{ce} = 8$ ;
- the competitive equilibrium trade volume  $q^{ce} \approx 73$ .



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## CE Welfare: Efficiency of Market Outcomes

**Consumer surplus** measures the sum of buyers' payoffs.

**Producer surplus** measures the sum of sellers' payoffs.

**Total surplus** is the sum of consumer and producer surplus.

Key features of CE in regular markets are:

- **total surplus is maximized** at CE prices;
- **cannot benefit some without hurting others** at CE outcome.

**Total surplus is maximized** at CE prices as

- low cost units are sold first;
- high value units are purchased first;
- trade volume depletes gains from trade.

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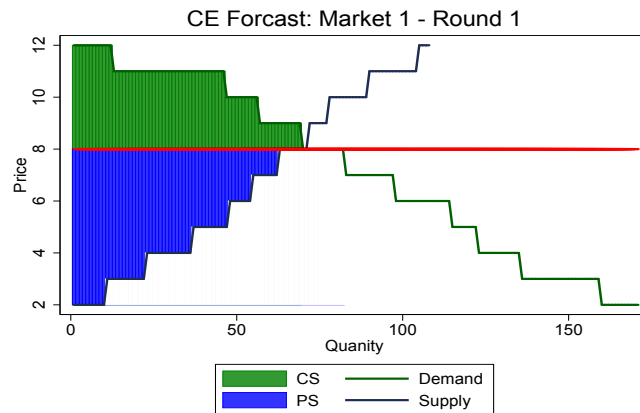
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## CE Welfare: Market 1 - Round 1

As in Problem Set 1, we can then compute:

- CE consumer surplus which amounts to  $CS = 183$ ;
- CE producer surplus which amounts to  $PS = 231$ .



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## CE Welfare: CE Surplus Across Markets

Theoretical surplus predictions across markets and rounds:

	Theory M1			Theory M2		
	CS	PS	TS	CS	PS	TS
Round 1	183	231	414	73	140	213
Round 2	187	247	434	70	151	221
Round 3	184	236	420	126	103	229

These are theoretical predictions that we will try to look for in the data!

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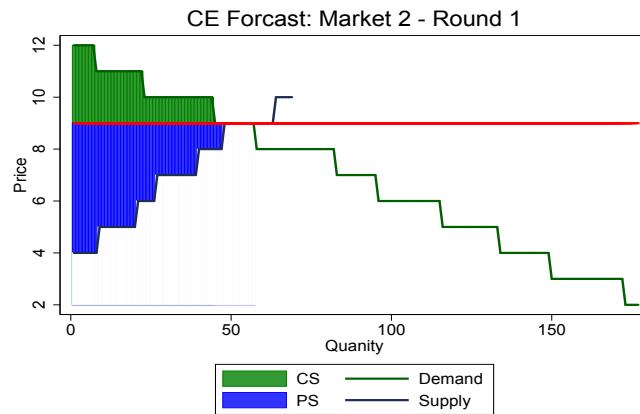
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## Comparative Statics: Market 2 - Round 1

In market 2 round 1,  $CS = 73$  and  $PS = 140$ :

- $CS$  and  $PS$  are smaller as the market has fewer units for sale;
- $PS$  is even smaller because the supply curve is flatter.



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## Experimental Evidence

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## Summary Statistics: DA Trading Prices

The table summarizes experimental prices across markets and rounds:

	Market 1			Market 2		
	$p^{ce}$	$p^{da}$	$SD$	$p^{ce}$	$p^{da}$	$SD$
Round 1	8	8.66	0.03	9	9.21	0.02
Round 2	8	8.43	0.03	9	8.88	0.05
Round 3	8	8.28	0.02	8	8.27	0.03

In the table in the market considered at the round considered:

- experimental prices amount to average trading prices;
- the standard deviation captures price volatility.

Across rounds, experimental prices converge to CE.

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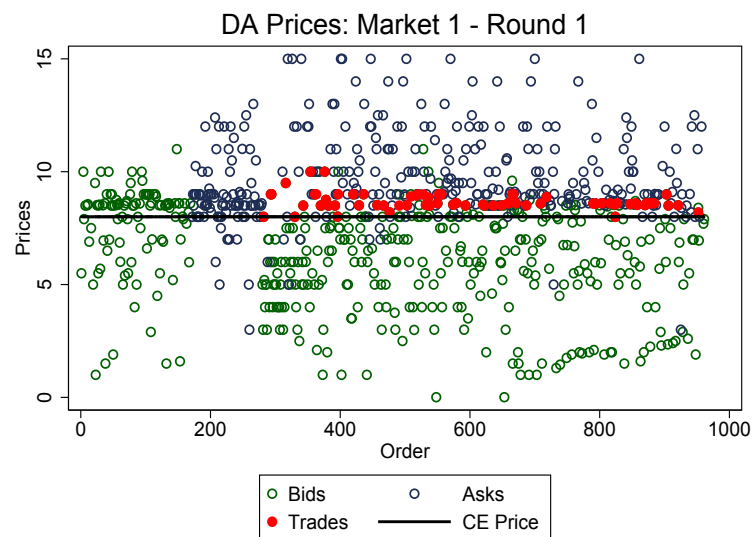
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## Bids, Ask & Prices: Market 1 - Round 1

The plot below depicts the time series of prices:



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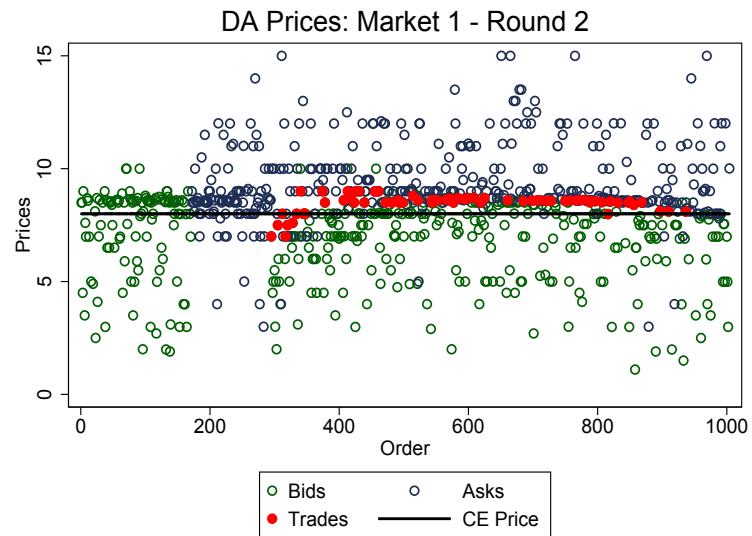
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## Bids, Ask & Prices: Market 1 - Round 2

The plot below depicts the time series of prices:



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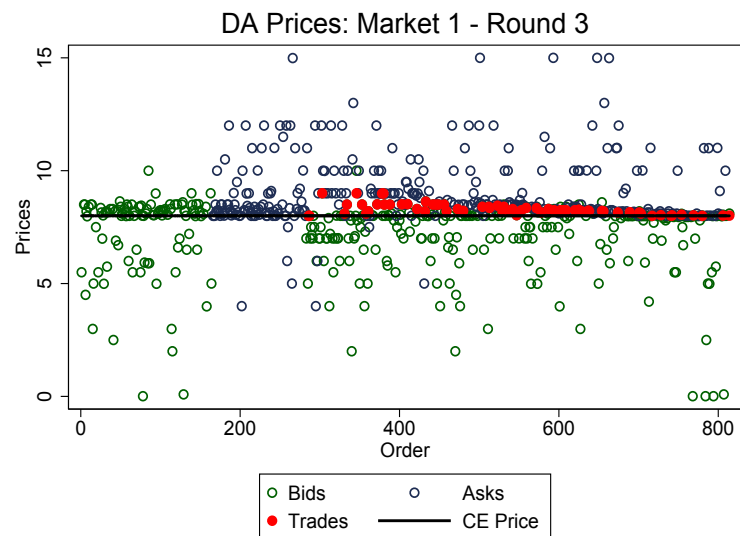
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## Bids, Ask & Prices: Market 1 - Round 3

The plot below depicts the time series of prices:



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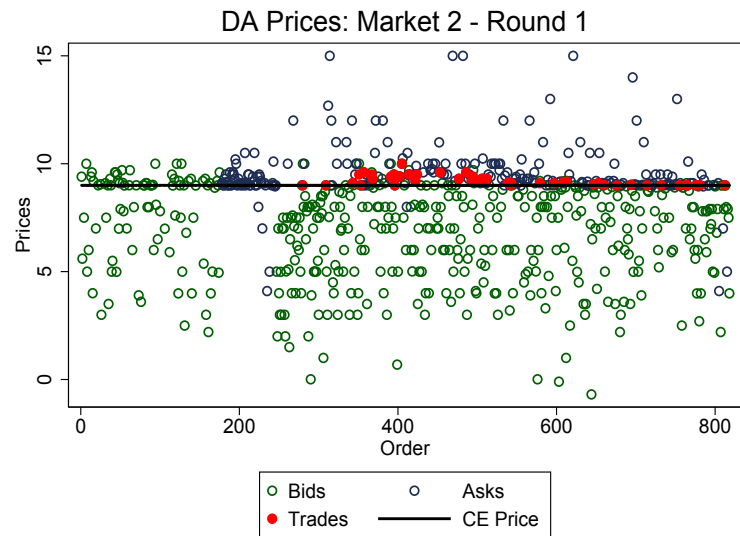
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## Bids, Ask & Prices: Market 2 - Round 1

The plot below depicts the time series of prices:



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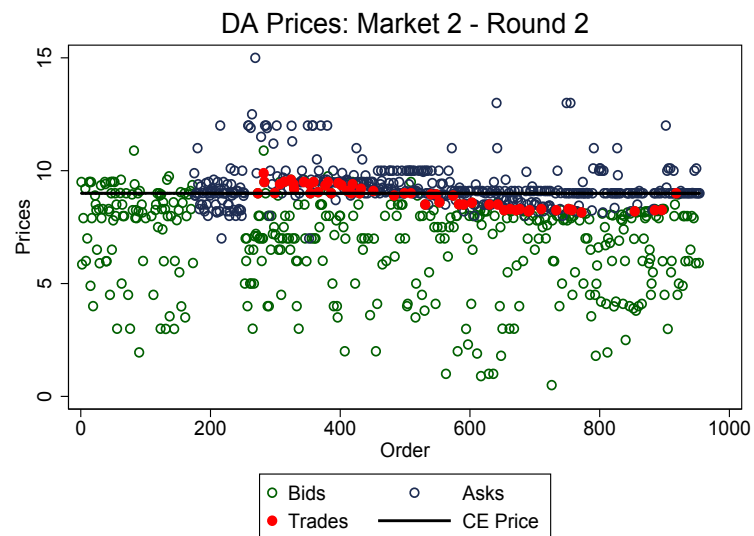
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## Bids, Ask & Prices: Market 2 - Round 2

The plot below depicts the time series of prices:



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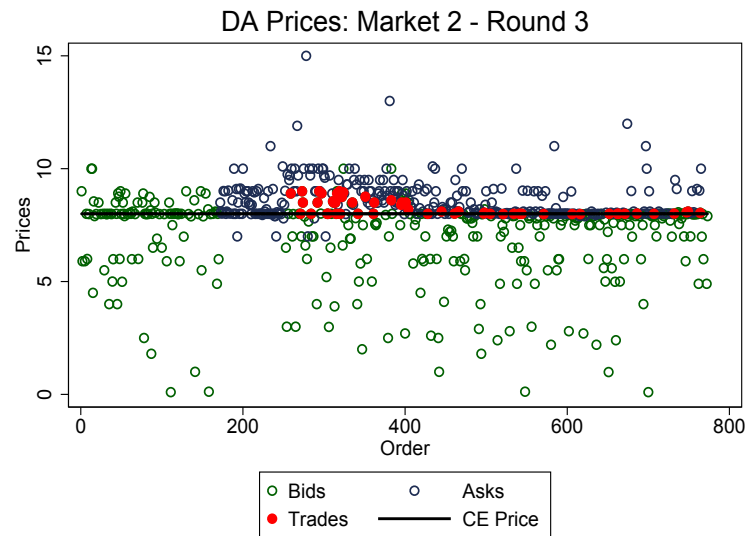
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## Bids, Ask & Prices: Market 2 - Round 3

The plot below depicts the time series of prices:



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## Summary Statistics: Surplus & Welfare Market 1

The following table summarize experimental surpluses:

	Theory M1			Data M1			Percent
	<i>CS</i>	<i>PS</i>	<i>TS</i>	<i>CS</i>	<i>PS</i>	<i>TS</i>	<i>TS</i>
Round 1	183	231	414	133	276	409	98.8%
Round 2	187	247	434	153	280	433	99.8%
Round 3	184	236	420	158	254	412	98.1%

In the table in the market considered at the round considered:

- consumer surplus amounts to the sum of buyers' payoffs;
- producer surplus amounts to the sum of sellers' payoffs;
- empirical surpluses match theoretical predictions.

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## Summary Statistics: Surplus & Welfare Market 2

The following table summarize experimental surpluses:

	Theory M2			Data M2			Percent
	CS	PS	TS	CS	PS	TS	TS
Round 1	73	140	213	63	132	195	91.6%
Round 2	70	151	221	77	144	221	100.0%
Round 3	126	103	229	109	118	227	99.1%

In the table in the market considered at the round considered:

- consumer surplus amounts to the sum of buyers' payoffs;
- producer surplus amounts to the sum of sellers' payoffs;
- empirical surpluses match theoretical predictions.

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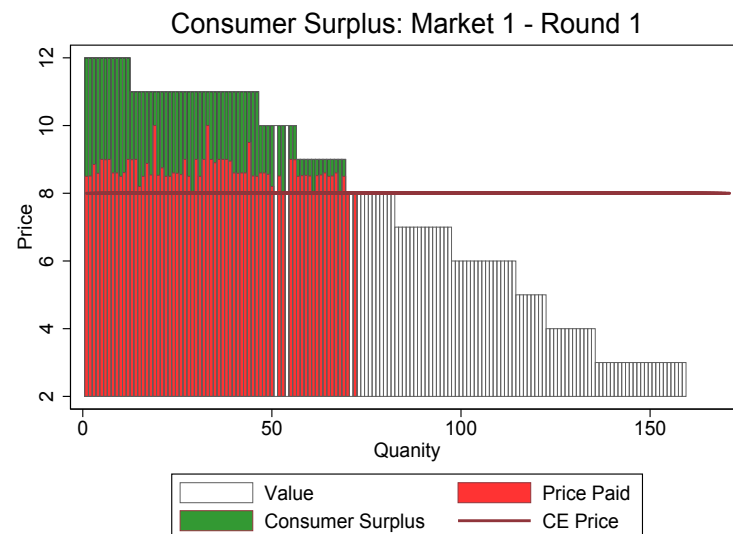
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## Consumer Surplus: Market 1 - Round 1

The plot below depicts experimental consumer surplus:



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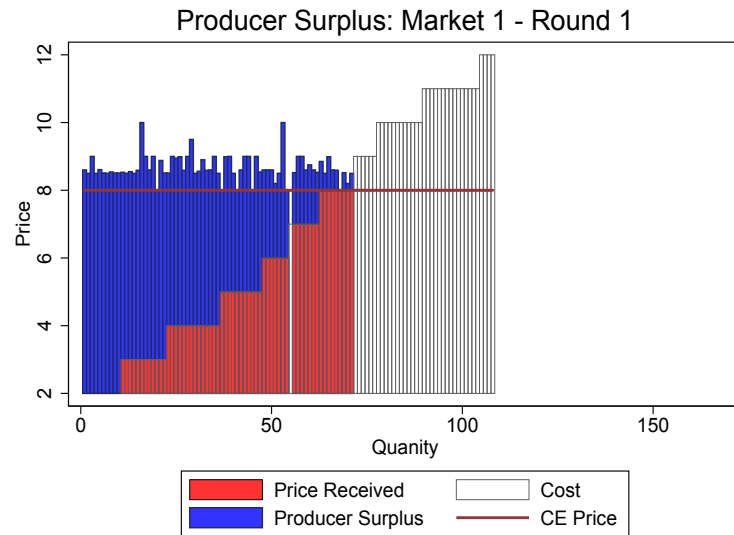
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## Producer Surplus: Market 1 - Round 1

The plot below depicts experimental producer surplus:



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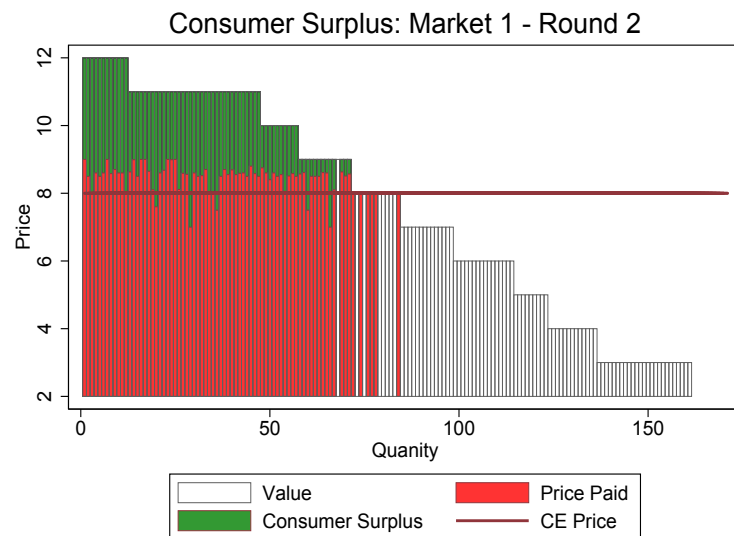
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## Consumer Surplus: Market 1 - Round 2

The plot below depicts experimental consumer surplus:



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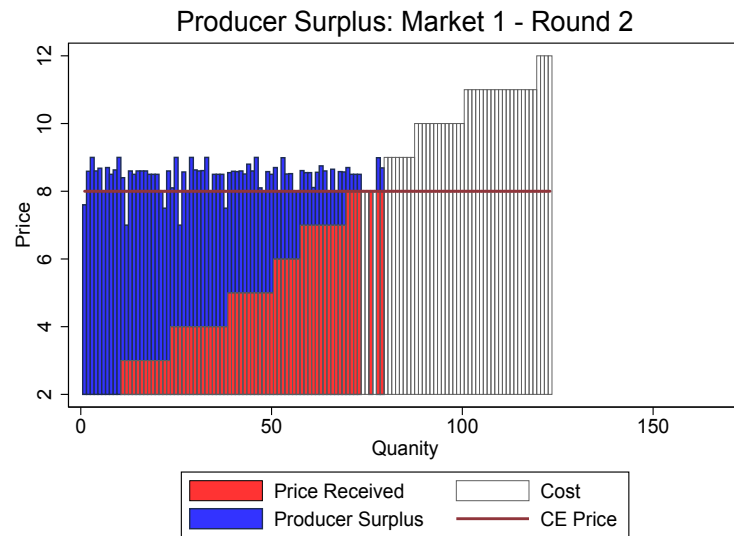
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## Producer Surplus: Market 1 - Round 2

The plot below depicts experimental producer surplus:



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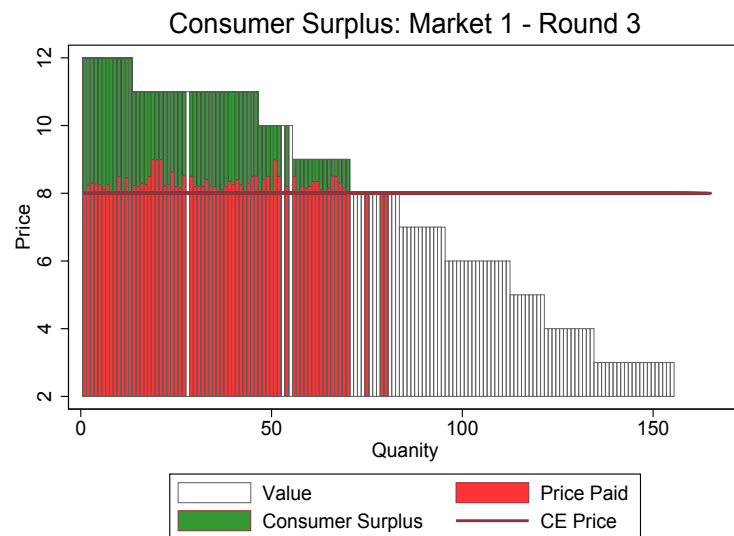
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## Consumer Surplus: Market 1 - Round 3

The plot below depicts experimental consumer surplus:



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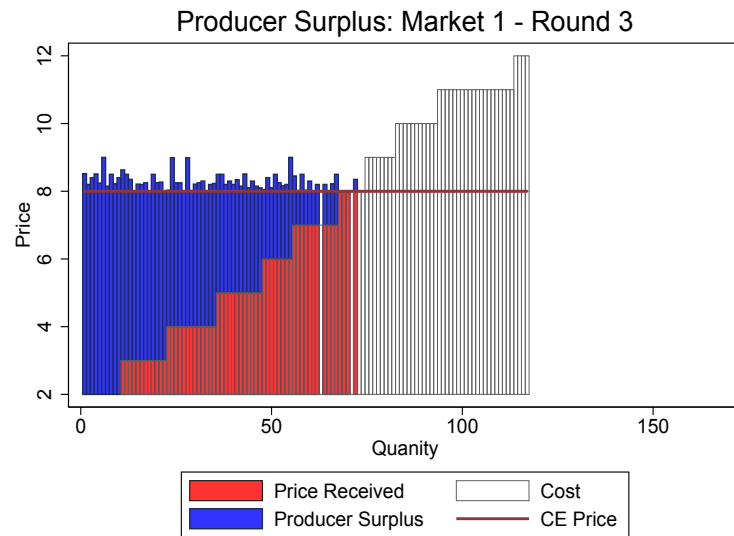
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## Producer Surplus: Market 1 - Round 3

The plot below depicts experimental producer surplus:



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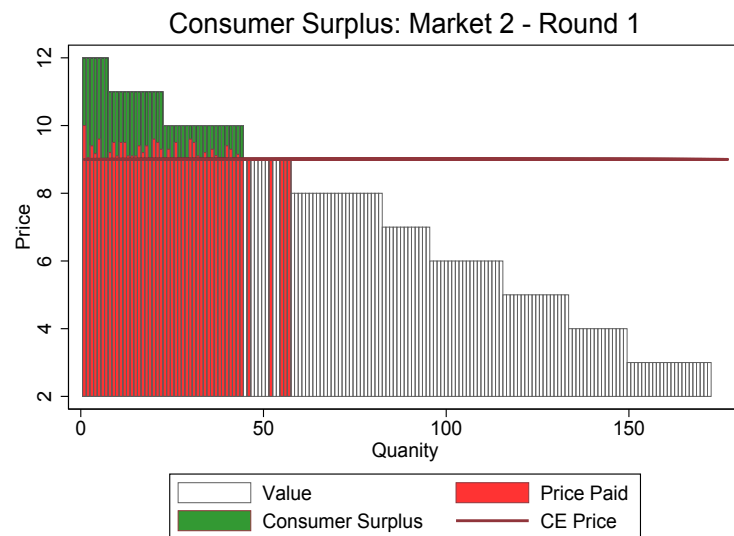
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## Consumer Surplus: Market 2 - Round 1

The plot below depicts experimental consumer surplus:



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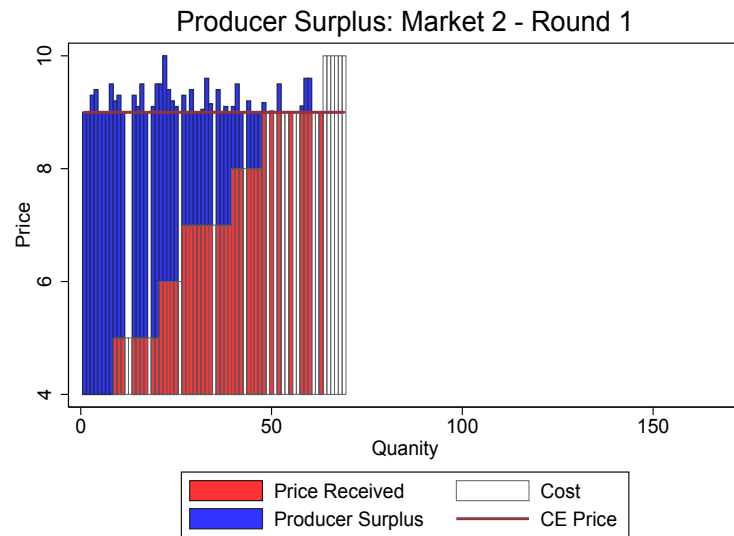
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## Producer Surplus: Market 2 - Round 1

The plot below depicts experimental producer surplus:



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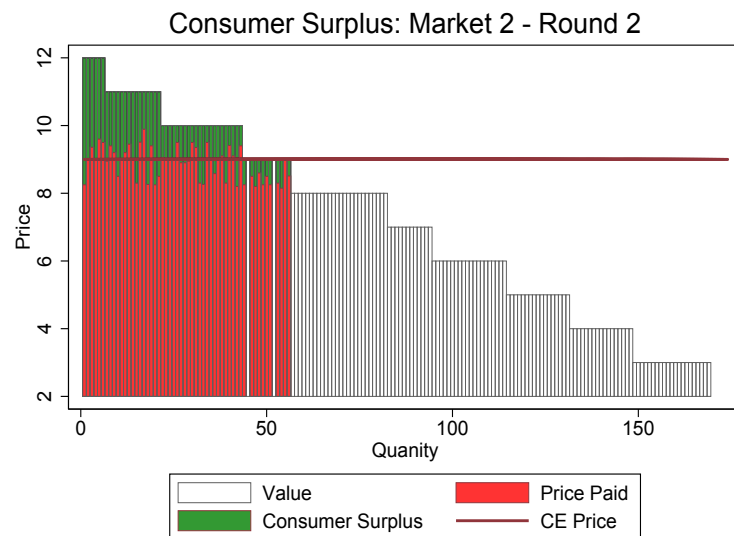
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## Consumer Surplus: Market 2 - Round 2

The plot below depicts experimental consumer surplus:



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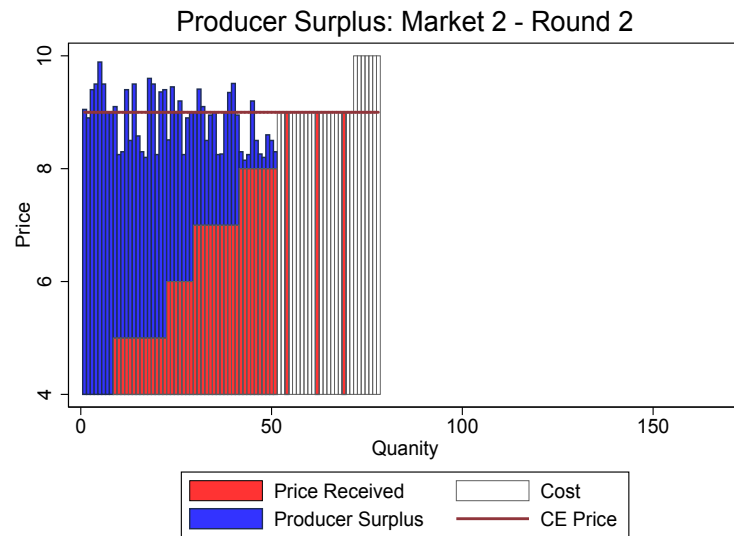
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## Producer Surplus: Market 2 - Round 2

The plot below depicts experimental producer surplus:



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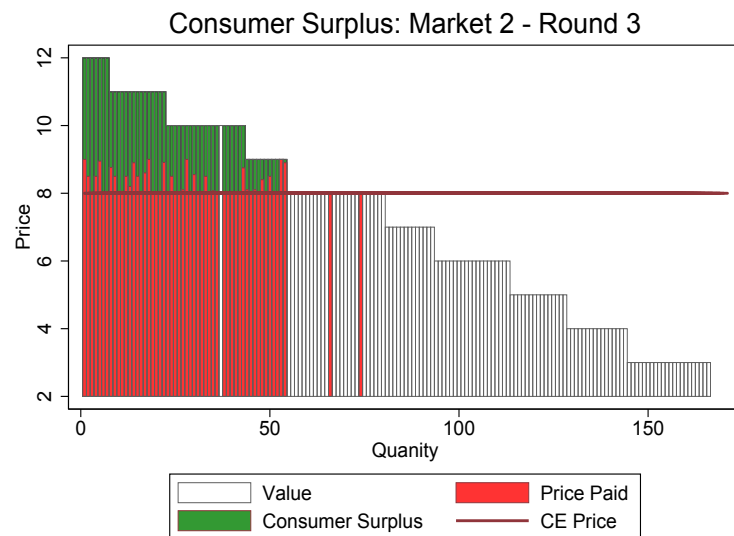
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## Consumer Surplus: Market 2 - Round 3

The plot below depicts experimental consumer surplus:



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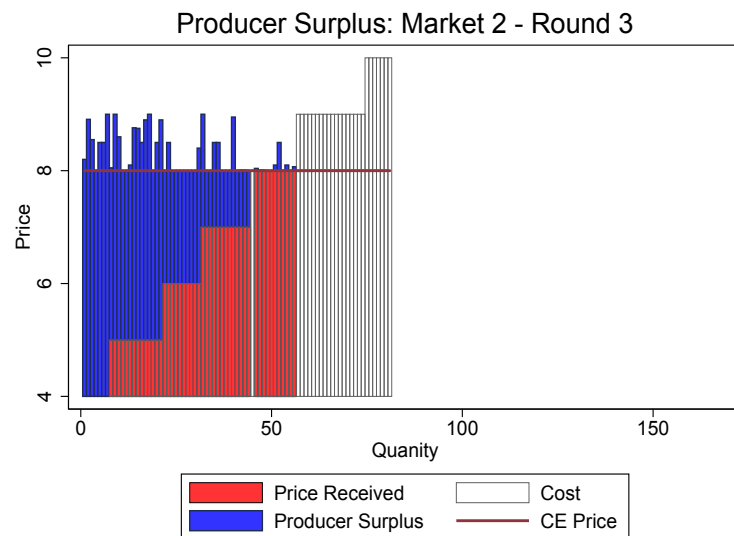
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## Producer Surplus: Market 2 - Round 3

The plot below depicts experimental producer surplus:



Levy & Nava (LSE)

Double Auction (Results)

MT 2017

33 / 47

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## Evidence Summary: Convergence to Competitive Pricing

As the previous plots elucidate in the Double Auction:

- price variation is limited;
- trade is approximately efficient;
- prices converge to CE prices within rounds;
- trade volume well approximates CE trade volume;
- the market converges to a competitive market across rounds.

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Levy & Nava (LSE)

Double Auction (Results)

MT 2017

34 / 47



# Decentralized Markets

## Decentralized Markets

**Decentralized Competition Models** presume that:

- the set of **feasible transactions is constrained**;
- **prices are determined by local bargaining**;
- **trade limitations** are a key determinant of price variation.

A host of models have been developed:

- **transaction costs models**;
- **search and matching models**;
- **spatial and networked models**...

These models are built to explain price variation within markets.

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Setting in which transaction costs uniformly reduce gains from trade:

- tend to limit trade relative to CE;
- tend to raise prices relative to CE.

In general though, raising transaction costs arbitrarily:

- has ambiguous local effect on trade volume relative to CE;
- has ambiguous local effect on prices relative to CE.

All of these settings deliver:

- considerable **price variation** relative to CE;
- a **smaller total surplus** relative to CE.

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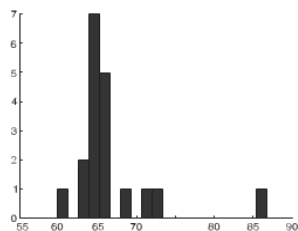
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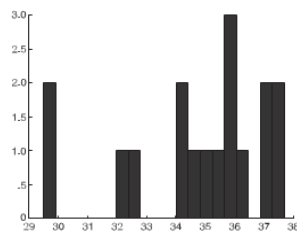
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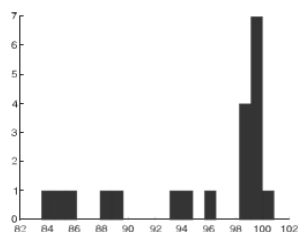
## Price Variation Evidence: Hong & Shum 2006



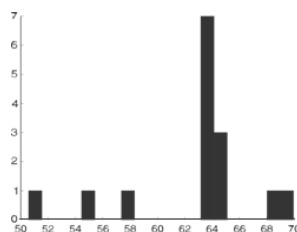
Stokey Lucas: Recursive Methods



Lazear: Personnel Economics



Billingsley: Probability & Measure



Duffie: Dynamic Asset Pricing

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# Effects of Centralization

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## Effects of Centralization: Prices

In the OTC Experiment, we found that:

	Round 1			Round 2		
	$p^{ce}$	$p^{otc}$	$SD$	$p^{ce}$	$p^{otc}$	$SD$
Market 1	5	7.51	1.10	8	6.86	1.04
Market 2	7	7.26	1.17	7	6.71	1.33
Market 3	7	6.91	0.94	7	6.50	1.09

In the Double Auction Experiment, we found that:

	Market 1			Market 2		
	$p^{ce}$	$p^{da}$	$SD$	$p^{ce}$	$p^{da}$	$SD$
Round 1	8	8.66	0.03	9	9.21	0.02
Round 2	8	8.43	0.03	9	8.88	0.05
Round 3	8	8.28	0.02	8	8.27	0.03

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## Effects of Centralization: Surplus

In the OTC Experiment, we found that:

	Round 1			Round 2		
	Theory	Data	Percent	Theory	Data	Percent
Market 1	41	–	–	244	165	67.6%
Market 2	368	269	73.1%	396	299	75.6%
Market 3	175	147	84.0%	187	61	32.7%

In the Double Auction Experiment, we found that:

	Market 1			Market 2		
	Theory	Data	Percent	Theory	Data	Percent
Round 1	414	409	98.8%	213	195	91.6%
Round 2	434	434	99.8%	221	221	100.0%
Round 3	420	412	98.1%	229	227	99.1%

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## Comparing Centralized to Decentralized Trade

Relative to the OTC game, in the DA game:

- there is **less dispersion in trade prices**;
- **prices are closer to CE** prices;
- **trade volume is closer to CE** trade volume;
- **surplus is closer to CE** surplus.

This concludes the first section of the course.

We now leave you with Erik who will talk about tax incidence.

Have a good first year at LSE!!

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# Omitted Plots

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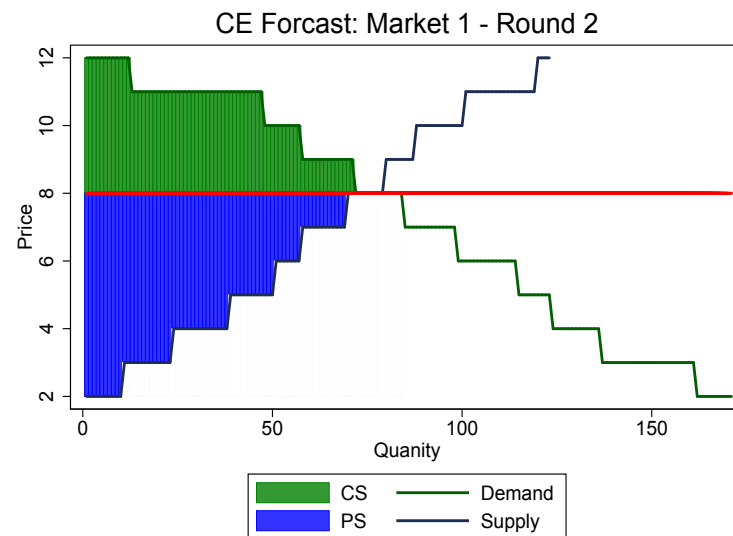
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## CE Outcome: Market 1 - Round 2

The plot below depicts the CE outcome:



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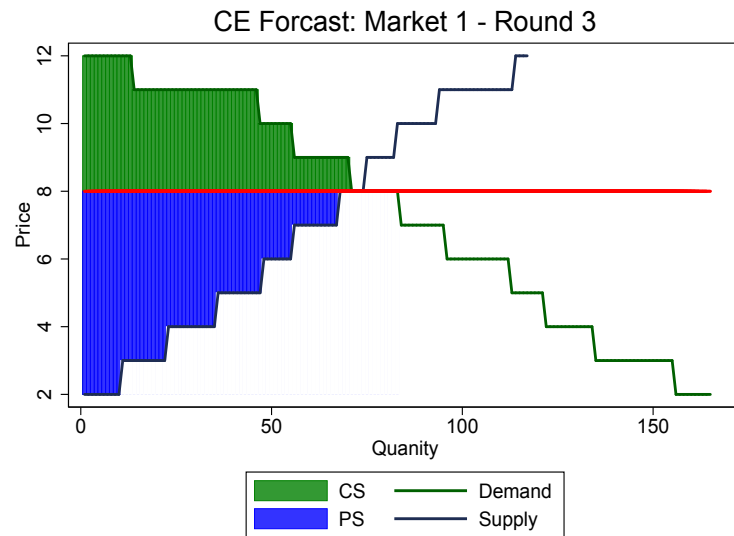
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## CE Outcome: Market 1 - Round 3

The plot below depicts the CE outcome:



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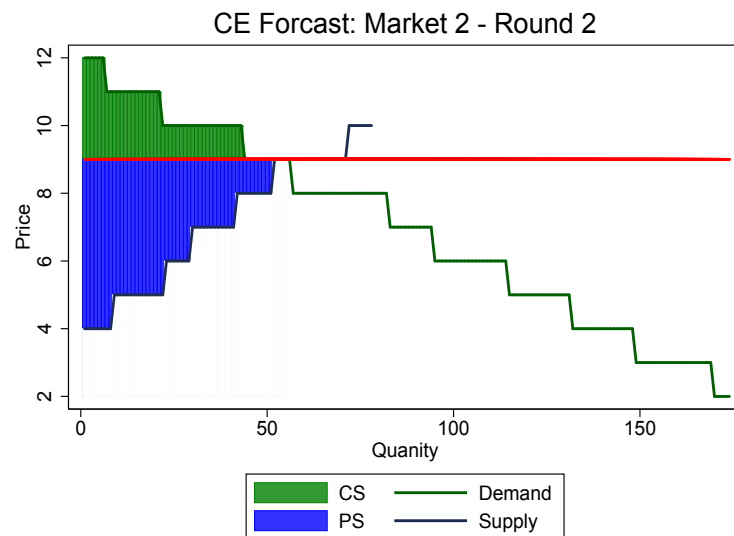
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## CE Outcome: Market 2 - Round 2

The plot below depicts the CE outcome:



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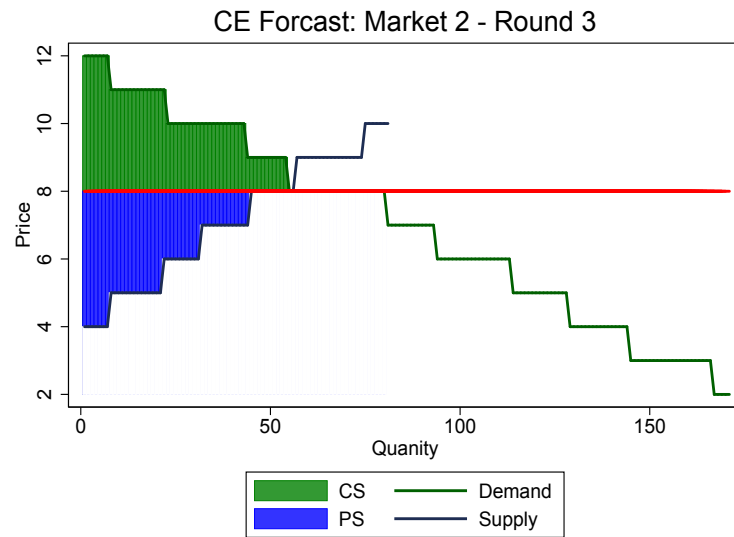
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## CE Outcome: Market 2 - Round 3

The plot below depicts the CE outcome:



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