

## LABOR MARKET FLOWS<sup>†</sup>

# The Ins and Outs of European Unemployment

By BARBARA PETRONGOLO AND CHRISTOPHER A PISSARIDES\*

In this paper we study the contribution of inflows and outflows to the dynamics of unemployment in three European countries, the United Kingdom, France, and Spain. All countries are interesting in their own right and in the comparison with each other. Britain's labor markets were strictly regulated up to the mid-1980s but they have been liberalized since then. France is still a regulated economy compared with Britain, with unemployment averaging about 8 percent. Spain has had the biggest rise in unemployment in Europe, reaching 24 percent in the mid-1990s, but policy reforms and fast growth since then brought it down to a level below that of France.

We compare performance in these three countries, making use of both administrative and labor force survey data. We find that the impact of the 1980s reforms in Britain is evident in the contributions of the inflow and outflow rates. The inflow rate became a bigger contributor after the mid-1980s, although its significance subsided again in the late 1990s and 2000s. In France the dynamics of unemployment are driven virtually entirely by the outflow rate, which is consistent with a regime with strict employment protection legislation. In Spain, however, both rates contribute significantly to the dynamics, very likely

as a consequence of the prominence of fixed-term contracts since the late 1980s.

### I. Accounting for the Dynamics of Unemployment

Several authors have recently addressed the question of unemployment dynamics. They follow a similar approach, albeit with some variations. Features that might differ across studies include (a) whether it is explicitly assumed that there are three states (employment, unemployment, and out of the labor force, henceforth, inactivity) or two (employment and unemployment); and (b) what "time aggregation" is used to deal with the fact that flows in and out of each state are taking place continually but data observations are taken at discrete times. Robert Shimer (2007) uses a method based on observations of short-term and long-term unemployment to deal with time aggregation in the two-state case. Michael Elsby, Ryan Michaels, and Gary Solon (2007) use a discrete-time variant of this procedure, based on the fact that the US Current Population Survey (CPS) uses the week as its reference period, with similar results. For the three-state case, Shimer uses an alternative procedure that has no analytical solutions for the three states, but has a solution for the two states. The latter is also used by Shigeru Fujita and Garey Ramey (2007), who deal with two states, and it is also the procedure that we follow in this paper.<sup>1</sup>

We make use of two types of data. The first is administrative data that record all the workers who join or leave an unemployment register during a period, usually a month. The definition of unemployment used in these data

<sup>†</sup> *Discussants:* Olivier Blanchard, Massachusetts Institute of Technology; Bruce Fallick, Federal Reserve Board; Michael Elsby, University of Michigan.

\* Petrongolo: Department of Economics and Centre for Economic Performance, London School of Economics, Houghton Street, London WC2A 2AE, UK (e-mail: b.petrongolo@lse.ac.uk); Pissarides: Department of Economics and Centre for Economic Performance, London School of Economics, Houghton Street, London WC2A 2AE, UK (e-mail c.pissarides@lse.ac.uk). We acknowledge with thanks research assistance from Alejandro Tamola and financial assistance from the Centre for Economic Performance, a designated research center of the Economic and Social Research Council. All data used in this paper can be downloaded from our personal Web sites.

<sup>1</sup> See Eran Yashiv (2006) for a discussion of these and other issues in the analysis of labor market dynamics based on flows.

usually covers workers who claim unemployment compensation or who are registered at government agencies. In Britain the unemployment series constructed in this way is known as the “claimant count.”

The second data source is the quarterly Labor Force Survey (LFS), which includes a rotating panel. In each quarter, we observe the state in which the worker belongs, and from this we construct the flows across the three states. This data source is similar to the CPS but it is quarterly and typically of much shorter duration.

Because the administrative data are for benefit claimants, it is biased toward workers who come from employment. When analyzing this series we therefore assume the existence of two states, employment and unemployment. We take from official sources the time series for monthly unemployment and new claims during the month, and make use of the identity linking the change in the stock to the difference in the rates to derive the outflow, to correct for small inconsistencies in the series. We then seasonally adjust the series using the X12 filter.

From the seasonally adjusted series, we compute continuous-time transition rates, assuming that these are constant during the month. Let  $t$  denote the month and  $\tau \in [0, 1)$  denote the time elapsed since the beginning of the current month. During month  $t$ , the continuous-time transition rate from unemployment to employment is  $f_t$  and that from employment to unemployment is  $s_t$ . The total unemployment outflow during  $t$ , denoted by  $F_t$ , is given by

$$(1) \quad F_t = (1 - e^{-f_t}) U_t + \int_0^1 [1 - e^{-f_t(1-\tau)}] S_{t+\tau} d\tau,$$

where  $U_t$  is unemployment at the start of the period and  $S_{t+\tau}$  is the unemployment inflow at  $t + \tau$ . Assuming that the unemployment inflow is uniform during the month gives

$$(2) \quad F_t = (1 - e^{-f_t}) U_t + \left(1 - \frac{1 - e^{-f_t}}{f_t}\right) S_t,$$

where  $S_t$  is the total inflow during the period. Equation (2) is solved for  $f_t$  using available data on  $F_t$ ,  $U_t$ , and  $S_t$ . Similarly, the unemployment inflow rate  $s_t$  can be obtained from

$$(3) \quad S_t = (1 - e^{-s_t}) N_t + \left(1 - \frac{1 - e^{-s_t}}{s_t}\right) F_t,$$

where  $N_t$  denotes employment at the beginning of period  $t$ .

With LFS data, we observe the labor force status of interviewees at quarterly intervals. In order to recover  $f_t$  and  $s_t$  we use the following relation between discrete- and continuous-time transition rates:

$$(4) \quad \hat{f}_t = \frac{f_t}{f_t + s_t} [1 - \exp(-f_t - s_t)],$$

$$(5) \quad \hat{s}_t = \frac{s_t}{f_t + s_t} [1 - \exp(-f_t - s_t)],$$

where  $\hat{f}_t$  is obtained by dividing the number of individuals who are unemployed in quarter  $t - 1$  and employed in quarter  $t$  by unemployment at  $t - 1$ , and  $\hat{s}_t$  is obtained by dividing the number of individuals who are employed in quarter  $t - 1$  and unemployed in quarter  $t$  by employment at  $t - 1$  (see Fujita and Ramey 2007, 4). Equations (4) and (5) can be solved for  $f_t$  and  $s_t$ .

Given the continuous-time  $f$  and  $s$ , the unemployment rate evolves according to  $\dot{u} = (1 - u)s - uf$ . Because  $s$  and  $f$  are large, under the assumption that  $s$  and  $f$  are constant during the period, unemployment practically converges to its steady state during the period. So changes in unemployment across periods are mainly driven by changes in the transition rates. Another way of stating this fact is to write actual unemployment as  $u = (s - \dot{u})/(s + f)$ . When comparing unemployment rates across periods, the differences due to the steady-state term  $s/(s + f)$  overwhelm the differences that might be due to differences in  $\dot{u}/(s + f)$  across periods.

We therefore approximate monthly unemployment by

$$(6) \quad u_t = \frac{s_t}{s_t + f_t}.$$

Computing directly the change  $u_t - u_{t-1} \equiv \Delta u_t$ , we obtain

$$(7) \quad \Delta u_t = (1 - u_t)u_{t-1} \frac{\Delta s_t}{s_{t-1}} - u_t(1 - u_{t-1}) \frac{\Delta f_t}{f_{t-1}}.$$

This is our key equation for accounting for the dynamic evolutions of unemployment in the two-state case.

With LFS data we can also take into account the third state, inactivity. Let  $f_{0t}$  and  $f_{1t}$ , respectively, be the transition rates from unemployment to inactivity and employment;  $s_{0t}$  and  $s_{1t}$  be the transition rates from employment to inactivity and unemployment; and  $e_{0t}$  and  $e_{1t}$  be the transition rates from inactivity to unemployment and employment. Then the steady-state conditions for unemployment and employment are

$$(8) \quad s_{1t}N_t + e_{0t}I_t = (f_{0t} + f_{1t})U_t,$$

$$(9) \quad f_{1t}U_t + e_{1t}I_t = (s_{0t} + s_{1t})N_t,$$

where all symbols have been defined except for  $I_t$ , which denotes inactivity in  $t$ . We solve these two equations for the conventional unemployment rate:

$$(10) \quad u_t \equiv \frac{U_t}{U_t + N_t} = \frac{s_{1t} + \frac{e_{0t}}{e_{0t} + e_{1t}}s_{0t}}{s_{1t} + \frac{e_{0t}}{e_{0t} + e_{1t}}s_{0t} + f_{1t} + \frac{e_{1t}}{e_{0t} + e_{1t}}f_{0t}},$$

and write it as

$$(11) \quad u_t = \frac{s_{1t} + i_{0t}}{s_{1t} + i_{0t} + f_{1t} + i_{1t}},$$

where  $i_{0t} \equiv e_{0t}s_{0t}/(e_{0t} + e_{1t})$  and  $i_{1t} \equiv e_{1t}f_{0t}/(e_{0t} + e_{1t})$  can loosely be interpreted as the contributions of inactivity transitions (respectively to unemployment and employment) to equilibrium unemployment.

Now, let  $s_t \equiv s_{1t} + i_{0t}$  and  $f_t \equiv f_{1t} + i_{1t}$ . Equation (11) becomes formally identical to (6) and so the decomposition in (7) holds.<sup>2</sup> Taking first differences,

<sup>2</sup> With three states, we cannot use simple closed-form solutions such as (4) and (5) in order to derive the continuous-time flow rates, so we do not correct for it. In the two-state model, correcting for time aggregation makes practically no difference to the results.

$$(12) \quad \frac{\Delta s_t}{s_{t-1}} = \frac{\Delta s_{1t}}{s_{1t-1} + i_{0t-1}} + \frac{\Delta i_{0t}}{s_{1t-1} + i_{0t-1}},$$

$$(13) \quad \frac{\Delta f_t}{f_{t-1}} = \frac{\Delta f_{1t}}{f_{1t-1} + i_{1t-1}} + \frac{\Delta i_{1t}}{f_{1t-1} + i_{1t-1}},$$

so the contributions of the total inflow and outflow rates can themselves be divided into terms that can respectively be attributed to the flows between employment and unemployment and the flows between employment and inactivity.

## II. United Kingdom

### A. Claimant Count Unemployment

The claimant count flows in Britain are quarterly in 1967–1983 and monthly since then. There have been some changes in definitions, most notably in 1983, but consistent time series based on the post-1983 definition are available.<sup>3</sup> The inflow includes all new claims during the quarter or month, and when combined with the stock of claimants yields the total outflow during the same period.

We work with quarterly averages of monthly data in order to remove excess volatility that may stem from measurement errors. Claimant count unemployment in our sample is always below the usual survey-based unemployment series (known in Britain as the LFS definition). But the two series move parallel to each other up to the late 1990s, when the gap widens—implying that the fraction of the unemployed who claim benefits is now lower. This change was due to the reform of the benefit system at the end of 1996, from “unemployment benefit” to the “job seekers allowance,” when the criteria for qualification were made more strict. The dynamic properties of the two series, however, are very similar to each other. Their correlation coefficient for the entire period is 0.991, and for

<sup>3</sup> The data source is the *Employment Gazette* for the pre-1983 period and NOMIS (<https://www.nomisweb.co.uk>) for the later period. Originally, the pre-1983 series included all registrations, in contrast to the post-1983 series, which includes only claimants. A small problem that remains is that before 1983 the series refer to Great Britain but after 1983 they refer to the United Kingdom.

the 1997–2007 period is 0.955. The steady-state series derived from (6) follows the claimant count series closely, except when unemployment is changing fast (recall that in general,  $u = (s - \dot{u})/(s + f)$ ).

The early series, up to 1983 for men only and without any correction for time aggregation, were analyzed by Pissarides (1986), who concluded that with the exception of the fast rise in unemployment in 1979–1981, fluctuations in unemployment were virtually entirely driven by fluctuations in the outflow rate. He studied this question by holding one of the rates constant at a time, and tracing the unemployment rate in (6) by allowing the other rate to take its observed values. The unemployment rate traced by holding  $s$  constant virtually coincided with the actual steady-state series. We address this issue here using the more informative breakdown in (7). Following Fujita and Ramey (2007, 7) we compare the contribution of the inflow and outflow rates by calculating the “beta values” of each of the two terms on the right-hand side of (7). We calculate

$$(14) \quad \beta_j = \frac{\text{cov}(\Delta u, \Delta u_j)}{\text{var}(\Delta u)} \quad j = s, f,$$

where  $\Delta u_s$  and  $\Delta u_f$  are, respectively, the contribution of  $s$  and  $f$  to the fluctuations in  $u$  shown in each of the two terms on the right side of (7). As  $\Delta u = \Delta u_f + \Delta u_s$ ,  $\beta_f + \beta_s = 1$ , and so in what follows we present results for  $\beta_s$  alone.

Table 1 shows this decomposition for the whole sample and four subperiods: the period up to 1982, when unemployment rose fast; the recovery period of 1985–1990; the brief recession of 1990–1993; and the long recovery and steady-state type of behavior since 1993. Because of some apparent inconsistencies in the data, we also report results derived by removing the quarters during which there was a big discrepancy between the change in actual unemployment and in the unemployment implied by flow equilibrium, which do not appear justified by economic events. We remove all quarters for which the discrepancy is more than 10 percent of actual unemployment, which number 11/160 observations.

In the early period, only 25–30 percent of the volatility in unemployment can be attributed to the inflow rate. The results in Pissarides (1986) are confirmed whichever method is used. A

TABLE 1—CONTRIBUTIONS FROM THE INFLOW RATE TO UNEMPLOYMENT VOLATILITY, UK CLAIMANT COUNT

Period	Feature	$\beta_s$	$\beta_s^*$
1967Q3–2007Q2	Whole sample	0.330	0.343
1967Q3–1982Q4	Big $u$ rise	0.275	0.286
1985Q1–1990Q2	Falling $u$	0.427	0.427
1990Q3–1993Q1	Rising $u$	0.454	0.595
1993Q2–2007Q2	Steady fall	0.250	0.202

Notes: In this and all subsequent tables,  $\beta_s$  is calculated as the ratio of the covariance between the contribution of the inflow rate and the change in steady-state unemployment to the variance of the change in steady-state unemployment.  $\beta_s^*$  is obtained after removing periods for which the difference between the change in steady-state unemployment and the change in actual employment was more than 10 percent of actual unemployment.

large change seems to have taken place, however, between 1985 and 1993, when the labor market reforms that deregulated the British market were put into place. The contribution of the inflow rate rises to about 45 percent and to an even bigger fraction when the data are purged of some odd observations. But surprisingly, although no policy reforms took place after 1993, the breakdown reverts to the one for the pre-1985 period.<sup>4</sup>

Looking at the direction of the dynamics of unemployment during the four subperiods, there is no apparent correlation between the direction of change and the contribution of each rate. For example, in the 1979–1982 recession, the rise in unemployment is driven by sharp falls in the outflow rate, with only a moderate increase in the inflow rate early on in the recession. In contrast, the rise in unemployment in the 1990–1993 recession is driven mainly by a rise in inflows, especially in the first four quarters of the recession. The patterns observed in the more recent recession parallel the ones observed in US recessions, as documented by Fujita and Ramey (2007).

A possible explanation for the relative importance of the outflow rate in the long recovery

<sup>4</sup> In the index of employment protection legislation constructed by Gayle Allard (2005), Britain is given 1.3 for the period 1985–1998, 1.4 before and after it, and higher values before 1979, on a scale from 0 to 5. The United States, for comparison, has an index value of 0.1 before 1989 and 0.6 after it. It is doubtful, however, that the small changes in the British time series can explain the large differences between subperiods in Table 1.

since 1993 is that the economy had features of a steady state during this period. Even in markets where it is easy to lay off labor, when the adjustments in the labor force required are small and labor turnover is high, it is easier for firms to implement adjustments through changes in their job creation rate, which drive the outflow rate.

### B. LFS Unemployment<sup>5</sup>

A rotating five-quarter panel for 1992–2005 can be extracted from the LFS files. Following the methodology outlined in Section I, we first compute the contribution of unemployment inflows and outflows to volatility under the assumption of two states only. The result is that for the long recovery of 1993Q2–2005Q3, the inflow rate contributes  $\beta_s = 0.483$ . The claimant count gives 0.250 for the contribution of inflows over the same period, which is substantially lower. Given that the LFS includes workers who transit via unemployment without benefit entitlement, this suggests that the volatility in noncompensated unemployment (young workers, new entrants, and re-entrants) is due much more to the entry into unemployment than is the volatility of benefit claimants. Since benefit claimants are likely to be older and more established workers, this makes sense. They are the ones more likely to be protected by employment legislation, union agreements, or seniority benefits on the job.

More interestingly, with LFS data, we can use the decomposition in (12) and (13) to take into account the contribution of the transitions between activity and inactivity. The contributions of each of the four rates are shown in Table 2. The comparisons between these numbers and the one in the two-state case should be with the contribution of the outflow calculated without time aggregation correction. This figure is 0.546.<sup>6</sup> In Table 2 the total contribution of the inflow into unemployment is  $0.352 + 0.133 = 0.485$ , so the approximate 50:50 split still holds. The transitions between activity and inactiv-

TABLE 2—CONTRIBUTIONS FROM FOUR TRANSITION RATES

Transition	UK	US
Employment-unemployment	0.352	0.325
Inactivity-unemployment	0.133	0.053
Unemployment-employment	0.364	0.588
Unemployment-inactivity	0.151	0.035

Notes: The column headed UK is from the UK LFS, 1993Q3–2003Q3. The US data are from Robert Shimer (see <http://robert.shimer.googlepages.com/flows>) and they are for the period 1967–2006.

ity contribute less than the transitions between employment and unemployment, but they still contribute a significant amount. Roughly two-thirds of the volatility in unemployment is due to the two-state transitions, evenly split, and the other third to the transitions between activity and inactivity, also evenly split between employment and unemployment.

There are no comparable calculations for the United States to compare with our numbers, so we calculated the  $\beta$  values of the four transition rates using Shimer's (2007) data from 1967 to 2006. The results are shown in Table 2. Perhaps surprisingly, the transitions between activity and inactivity contribute much less to unemployment volatility in the United States than in the United Kingdom. The contribution of the job exit rate is about the same in the two countries, with the slack left over by the lower inactivity contributions in the United States taken up by the job finding rate.

## III. Continental Europe

### A. France

For France, we use claimant data, which are available monthly since 1991. The average unemployment rate obtained with claimant data is only 0.3 percentage points lower than the official one, based on the International Labour Organisation (ILO) definition, and the coefficient of correlation between the two is 0.941. The continuous time transition rates are obtained from (2) and (3), and deliver an equilibrium unemployment rate that is very closely correlated with the actual one (0.964).

The unemployment rate in France starts off high, between 10 percent and 12 percent in the early 1990s, then falls to just below 8 percent

<sup>5</sup> For more discussion of LFS-derived flows in Britain, see Pedro Gomes (forthcoming)

<sup>6</sup> This is instead of the one we reported above, 0.483. As emphasized by a number of authors, time aggregation tends to reduce the contribution of the inflow rate. See, for example, Elsbey, Michaels, and Solon (2007) for more discussion.

TABLE 3—CONTRIBUTIONS FROM THE INFLOW RATE TO UNEMPLOYMENT VOLATILITY, FRENCH CLAIMANT COUNT

Period	Feature	$\beta_s$
1991Q2–1996Q4	Whole sample	0.201
1991Q2–1996Q4	Untrended $u$	0.053
1997Q1–2001Q2	Falling $u$	0.449
2001Q3–2007Q3	Untrended $u$	0.088

between 1997 and 2001, and finally it fluctuates around 8 percent in the last six years. There is thus one important expansion in the French economy, linking two periods of roughly constant unemployment. Table 3 shows the relative contribution of the inflow rate to the volatility of equilibrium unemployment. The reported values of  $\beta_s$  indicate that the outflow is responsible for virtually all the unemployment volatility when unemployment is roughly untrended. In contrast, in the strong expansion of the late 1990s, inflows and outflows contribute about the same to unemployment volatility. Values of  $\beta_s^*$  are not reported, as there were no observations with a large discrepancy between the actual and predicted change in unemployment.

France has strict employment protection legislation, having Allard (2005) index of 3 during our sample period. So it is not surprising that the employment-unemployment transition contributes less to cyclical volatility. In the expansion period of 1997–2001, it contributes more, but it is falling, so employment protection is not binding. This contrasts with Britain, where in the low regulation period after 1985, the contribution of the inflow rate is about the same in both expansions and contractions.

### B. Spain

Available claimants data for Spain are not suitable for our purposes, so we use individual record files from the Spanish LFS, which is available as a six-quarter panel since 1987. We recover continuous-time transition rates solving (4) and (5), and the resulting equilibrium unemployment has a correlation coefficient with actual unemployment of 0.974.

Spain has had, until very recently, the highest (by far) unemployment rate in Europe. In 1987 Spanish unemployment was about 20 percent, and after a mild fall it rose to reach a record 24 percent in 1994. Then it started a very long,

TABLE 4—CONTRIBUTIONS FROM THE INFLOW RATE TO UNEMPLOYMENT VOLATILITY, SPANISH LFS

Period	Feature	$\beta_s$	$\beta_s^*$
1987Q4–2006Q4	Whole sample	0.433	0.538
1990Q4–1994Q1	Rising $u$	0.627	0.644
1994Q2–2006Q4	Steady fall	0.392	0.461

TABLE 5—CONTRIBUTIONS FROM FOUR TRANSITION RATES, SPANISH LFS

Transition	Whole sample	1990Q4–1994Q1	1994Q2–2006Q4
Employment-unemployment	0.299	0.402	0.230
Inactivity-unemployment	0.133	0.218	0.092
Unemployment-employment	0.348	0.223	0.337
Unemployment-inactivity	0.220	0.157	0.341

steady fall, and is currently below both French and German unemployment. A feature of the Spanish employment expansion is that after the mid-1980s, the majority of new matches were on the basis of fixed-term contracts, with maximum duration of three years. This policy was introduced to counteract the strict employment protection characterizing Spanish labor markets (with an Allard index of 3.2 declining to 2.3 during the sample period). By the early 1990s, as much as 90 percent of new job creation and 30 percent of employment was with fixed-term contracts. Although the use of fixed-term contracts started to be regulated in 1994, and more so after 1997, this regulation did not have much impact on their incidence in the Spanish labor market.

The contribution of the inflow rate that we calculated for Spain on the assumption of two states only is shown in Table 4. Over the whole sample period, inflows and outflows contribute in nearly equal parts to unemployment volatility (whether or not one drops observations with inconsistent changes in actual and predicted unemployment). But during the strong rise in unemployment between 1990 and 1994, the inflow accounts for over 60 percent of unemployment volatility. Virtually all job separations during this period were due to expiring fixed-term contracts. The outflow accounts for almost two-thirds of the following 12-year-long expansion.

Table 5 reports results of the decomposition in (12) and (13), when inactivity is explicitly taken into account. Over the whole period, the contribution of inactivity transitions in Spain is about the same as in Britain, with the unemployment-inactivity transition playing a slightly bigger role. But there are differences in the two subperiods of our sample, with the transition from inactivity to unemployment becoming more important in the recession of the first subperiod, and the unemployment-inactivity transition becoming more important in the recovery of the second period.

#### REFERENCES

- Allard, Gayle.** 2005. "Measuring Job Security Over Time: In Search of a Historical Indicator." Instituto de Empresa Working Paper WP-05.
- Elsby, Michael, Ryan Michaels, and Gary Solon.** 2007. "The Ins and Outs of Cyclical Unemployment." Unpublished.
- Fujita, Shigeru, and Garey Ramey.** 2007. "The Cyclicalities of Separation and Job Finding Rates." Federal Reserve Bank of Philadelphia Working Paper 07-19.
- Gomes, Pedro.** Forthcoming. "Labour Market Flows in the United Kingdom." Bank of England Discussion Paper.
- Pissarides, Christopher A.** 1986. "Unemployment and Vacancies in Britain." *Economic Policy*, 3(3): 499-559.
- Shimer, Robert.** 2007. "Reassessing the Ins and Outs of Unemployment." Unpublished.
- Yashiv, Eran.** 2006. "US Labor Market Dynamics Revisited." IZA Discussion Paper 2445.

**This article has been cited by:**

1. Ching-Yang Lin, Hiroaki Miyamoto. 2011. Gross Worker Flows and Unemployment Dynamics in Japan. *Journal of the Japanese and International Economies* . [[CrossRef](#)]
2. Christopher A. Pissarides. 2011. Equilibrium in the Labor Market with Search Frictions. *American Economic Review* **101**:4, 1092-1105. [[Citation](#)] [[View PDF article](#)] [[PDF with links](#)]
3. Jennifer C. Smith. 2011. The Ins and Outs of UK Unemployment\*. *The Economic Journal* **121**:552, 402-444. [[CrossRef](#)]
4. Hiroaki Miyamoto. 2011. Cyclical behavior of unemployment and job vacancies in Japan. *Japan and the World Economy* . [[CrossRef](#)]