

## Appendix: Some tax arithmetic

This provides some back of the envelope calculations to assess the impact of an environmental tax reform on disposable income of wage earners; i.e. a reduction wage taxes paid for by increased taxes on (polluting) energy consumption. In the extreme case of a reduction of the wage tax to zero the change in income for the representative wage earner is

$$\Delta = I_W \tau_W - EE_W \tau_E$$

where  $I_W$  is (pre tax) wage income,  $EE_W$  energy expenditure of wage earners,  $\tau_W$  and  $\tau_E$  the tax rates on wage income and energy expenditure respectively. In order to balance the budget the government must impose an energy tax rate of

$$\tau_E = \frac{I_W}{(EE_W + EE_O)} \tau_W$$

where  $EE_O$  is energy expenditure paid for by non-wage income.<sup>1</sup> Combining these two equations yields percentage effect on post tax wage income of a revenue neutral environmental tax reform as:

$$\frac{\Delta}{(1 - \tau_W)I_W} = \frac{\tau_W}{1 - \tau_W} \left( 1 - \frac{EE_W}{EE_W + EE_O} \right)$$

For  $\tau_W$ , current tax rate on earnings I assume 32% which is based on calculations by [Patrick Minford for the UK](#). The share of energy expenditure by wage income in total energy expenditure we can rewrite as

$$\frac{EE_W}{EE_W + EE_O} = \left( 1 + \frac{e_O}{s_W e_W} \right)^{-1}$$

where  $s_W$  is the wage share of total income,  $e_W$  and  $e_O$  the share of energy spending for wage income and other income respectively. For  $s_W$  I am assuming 0.6.<sup>2</sup> Using the ratio between the bottom and top deciles of income distribution from Wier et al. (see Footnote 4) I am using  $\frac{e_O}{e_W} = 0.5$ . This yields an increase of 21% for post tax wage income.

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<sup>1</sup> I am assuming here that while taxes might alter employment and/or energy consumption levels they do not impact on expenditure. This is consistent with Cobb Douglas production and utility functions and for expositional simplicity. The argument extends to more general cases.

<sup>2</sup> This is roughly consistent with the figures provided in Serres, A. D., Scarpetta, S., and Maisonneuve, C. D. L. (2001). Falling wage shares in Europe and the United States: How important is aggregation bias? *Empirica*, pages 375-401.